

# WICHITA STATE UNIVERSITY

Department of Mathematics, Statistics & Physics 7.6 (P) emailed

ch number increases. Such

a Brownian particle from a

$z_0$  in a planar domain  $D$ . C. What is the chance, denoted  $h_{z_0}(r)$ , that the particle's first exit from  $D$  occurs within a fixed distance  $r > 0$  of  $z_0$ ? The function of  $r$  suggested by this question, denoted  $h_{z_0}:[0, \infty) \rightarrow [0,1]$ , is called the harmonic measure distribution function, or h-function, of  $D$  with respect to  $z_0$ . We can think of the h-function as a signature that encodes the geometry of the boundary of  $D$ . In the language of PDEs, the h-function can also be formulated in terms of a suitable Dirichlet problem on  $D$ . For simply connected domains, the theory of h-functions is now quite well developed and several explicit results are known. However, until recently, for multiply connected domains the theory of h-functions has been almost entirely out of reach.

The special function theory employed when solving the two aforementioned problems is centered around the so-called Schottky-Klein prime function, a special transcendental function which plays a central role in problems involving multiply connected domains (i.e. domains with multiple boundary components). Despite this, it has been scarcely used - until relatively recently - by both pure and applied mathematicians since it was originally written down (independently by both Schottky and Klein towards the end of the 19th century).

## Friday, September 21, 2018

## 3:00 PM in 372 Jabara Hall

*Please come join us for refreshments before the lecture at 2:30 p.m. in room 353 Jabara Hall.*